

1 **A statistical shape model of the tibia-fibula complex: sexual**
2 **dimorphism and effects of age on reconstruction accuracy from**
3 **anatomical landmarks**

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21 **A statistical shape model of the tibia-fibula complex: sexual**
22 **dimorphism and effects of age on reconstruction accuracy from**
23 **anatomical landmarks**

24 A statistical shape model was created for a young adult population and used to
25 predict tibia and fibula geometries from bony landmarks. Reconstruction errors
26 with respect to CT data were quantified and compared to isometric scaling. Shape
27 differences existed between sexes. The statistical shape model estimated tibia-
28 fibula geometries from landmarks with high accuracy (RMSE = 1.51-1.62 mm),
29 improving upon isometric scaling (RMSE = 1.78 mm). Reconstruction errors
30 increased when the model was applied to older adults (RMSE = 2.11-2.17 mm).
31 Improvements in geometric accuracy with shape model reconstruction changed
32 hamstring moment arms 25-35% (1.0-1.3 mm) in young adults.

33 Keywords: lower extremity; bone; musculoskeletal model; participant-specific

34 **Introduction**

35 Musculoskeletal models are commonly used to estimate muscle forces and joint
36 kinematic and kinetic parameters associated with human movement. Outputs from
37 musculoskeletal models (e.g., muscle moment arms and joint contact forces) are highly
38 sensitive to bone geometry (Scheys et al. 2008; Gerus et al. 2013; Clouthier et al. 2019;
39 Ding et al. 2019; Xu et al. 2020), which is frequently defined using either participant-
40 specific imaging or model scaling approaches. Advanced imaging, including computed
41 tomography (CT) and magnetic resonance imaging, is the gold standard for quantifying
42 participant-specific bone geometry. Of course, CT imaging requires ionizing radiation
43 and both imaging modalities are costly and can be challenging to acquire. Consequently,
44 it is more common to scale a ‘generic’ musculoskeletal model according to gross
45 anthropometric measurements (Delp et al. 1990; Arnold et al. 2010), which does not
46 necessarily capture potentially important differences in bone geometry among
47 individuals.

48 Statistical shape models (SSM) provide an alternative method to incorporate
49 participant-specific bone geometry into musculoskeletal models. A SSM numerically
50 calculates the average and principal modes of variation of a shape (e.g., bone geometry)
51 from a training set of models (Audenaert et al. 2019). These models can be used to
52 reconstruct participant-specific geometry from incomplete information by morphing the
53 average shape along the modes of variation to best fit the target data. In this way, the
54 pelvis, femur, tibia-fibula complex, and multiple bones of the foot have been
55 reconstructed from select anatomical landmarks identified either on the bone surface or
56 using skin-mounted motion capture markers (Zhang et al. 2016; Grant et al. 2020; Nolte
57 et al. 2020).

58 Bone geometry is known to vary as a function of age and sex, among other factors
59 (Ruff & Hayes 1988; Stevens & Vidarsdóttir 2008; Mahfouz et al. 2012; Li et al. 2014;
60 Brzobohatá et al. 2015; Brzobohatá et al. 2016; Audenaert et al. 2019). Indeed, periosteal
61 expansion increases with age, although to a lesser degree in females than males (Ruff &
62 Hayes 1988; Jee 2001). At the tibia, observed geometric differences between males and
63 females include: greater protrusion of the tibial tuberosity, diaphyseal curvature,
64 diaphyseal cross-sectional properties (Smock et al. 2009; Feldman et al. 2012; Sherk et
65 al. 2012), condyle size (Mahfouz et al. 2012; Audenaert et al. 2019; Tümer et al. 2019),
66 and metaphyseal slope (Brzobohatá et al. 2015; Brzobohatá et al. 2016). These
67 differences have been used to classify bones into age and sex- specific groups with 61.0-
68 98% accuracy, depending on the study (Stevens & Vidarsdóttir 2008; Brzobohatá et al.
69 2015; Brzobohatá et al. 2016; Audenaert et al. 2019).

70 Previous studies reconstructing the tibia-fibula complex from anatomical markers
71 used participant groups with wide age ranges (20-70 years in Nolte et al. (2020) and 15-
72 92 years in Zhang et al. (2016)) to train and test the SSMs. While these SSMs may be

73 more widely generalizable, a model more specific to a population of interest such as
74 young healthy adults - a commonly used group in biomechanics modelling studies - may
75 provide more accurate results. Furthermore, these studies have not investigated how
76 errors in shape influence musculoskeletal modelling parameters. Thus, the primary
77 purpose of this study was to evaluate the accuracy of tibia-fibula complex reconstructions
78 from anatomical bony landmarks using a SSM developed for a healthy young adult
79 population, and quantify the subsequent effects on muscle moment arms. Errors
80 associated with isometrically scaling the average model were also quantified for
81 comparison. In line with previous literature (Zhang et al. 2016; Nolte et al. 2020), we
82 hypothesized that reconstruction errors would be smaller for the SSM-generated
83 geometries compared to isometric scaling. The secondary objectives of this study were
84 (1) to quantify sex differences in bone geometry, and (2) to evaluate the generalizability
85 of the developed young adult SSM to older adults. We expected to observe differences in
86 size and shape between young adult males and females. Due to age-related differences in
87 bone geometry, we hypothesized that reconstruction errors and changes in muscle
88 moment arms would be larger for the older adults.

89 **Materials and methods**

90 ***Model development:***

91 Forty-one physically active participants (22 F and 19 M, 18-23 years, physically active at
92 least three times per week) were recruited to obtain a range of statures (mean (range),
93 female: 1.66 m (1.49 – 1.80 m), 59.7 kg (47.7-71.8 kg), male: 1.77 m (1.62 – 1.87 m),
94 71.8 kg (60.0 – 83.7 kg)). CT scans of the left lower leg were obtained using a GE
95 Revolution GSI (GE Healthcare, Waukesha, WI) with image acquisition settings of 120
96 kVp and 180 mA. Images were reconstructed with an in-plane resolution of 0.488 mm x

97 0.488 mm and a slice thickness of 0.625 mm. Ethics approval was obtained from the
98 university's Conjoint Health Research Ethics Board and written, informed consent was
99 obtained from each participant prior to scanning.

100 The tibia and fibula geometries were segmented using a semi-automatic procedure
101 and surface meshes were created in the Mimics Innovation Suite (v21, Materialise,
102 Leuven, Belgium). Nodal correspondence and registration were performed in MATLAB
103 (R2020a, Mathworks, MA, USA). A template mesh was selected, corresponding to an
104 individual with tibia/fibula surface area close to the sample mean, and contained 3874
105 and 2111 nodes for the tibia and fibula, respectively. A sensitivity analysis, evaluating
106 shape errors resulting from the template deformation step, was used to determine the
107 number of nodes for the tibia and fibula. Nodal correspondence between meshes was
108 established using the Coherent Point Drift algorithm (Myronenko & Song 2010). This
109 algorithm performs translation, rotation, scaling, and local deformation to match a
110 moving point-set (template) to a fixed point-set (participant surface). A nearest
111 neighbours algorithm was used to identify corresponding points. A preliminary analysis
112 of nodal correspondence registration errors and the number of principal components
113 needed to explain 95% of the variance demonstrated these measures were insensitive to
114 the choice of template. Tibia and fibula point clouds were then combined and rigidly
115 aligned using a generalized Procrustes analysis that retained bone size. The tibia and
116 fibula were modelled together to include relative positioning between the two bones
117 within the model.

118 A principal component analysis (PCA) was applied to the registered data to obtain
119 the average shape and modes of variation (i.e., principal components) for the sample. An
120 analysis described by Mei *et al.* (2008) evaluating bootstrap stability on mode direction
121 and comparison with noise was used to determine the number of principal components to

122 retain. Eight principal components accounting for 96.2% of the total variance in the
123 model were ultimately retained. Scores for each retained principal component were
124 compared using unpaired t-tests to determine if and how size and shape differed between
125 sexes (SPSS v.26, IBM, NY, USA, $\alpha = 0.05$). Centroid size, the square root of the sum of
126 squared Euclidean distances of all points in a shape from the centroid of the shape, was
127 calculated. Pearson correlations were used to evaluate whether principal component
128 scores were correlated with size.

129 ***Landmark-based reconstruction:***

130 The tibia-fibula SSM meshes were reconstructed based on two sets of anatomical
131 landmarks (Figure 1). The first set contained nine landmarks that could be identified
132 through palpation, and thus used to estimate tibia and fibula geometries from skin-
133 mounted motion capture markers: tibial tuberosity, medial condyle, lateral and medial
134 malleoli, lateral aspect of the head of the fibula, anterior border of the tibia at 25%, 50%
135 and 75% of the distance between the medial condyle and malleolus markers, lateral fibula
136 diaphysis at 25% of the distance from the lateral malleolus to the lateral point on the head
137 of the fibula. The second set contained the nine “palpable” landmarks described above as
138 well as another five landmarks that could not be palpated, but could be captured through
139 imaging, to determine if additional information regarding dimension and curvature
140 improved reconstruction accuracy: posterior aspect of the medial condyle, posterior
141 aspect of the mid-diaphysis (50%) of the tibia, apex of the fibular head, fibular diaphysis
142 at 50% (posterior) and 85% (anterior) of the distance between the lateral malleolus and
143 the lateral point on the fibular head. Both sets of landmarks (Figure 1) were manually
144 digitised on the average shape as well as each participants’ CT-based bone surface meshes
145 in MATLAB (R2020a, Mathworks, MA, USA).

146 A leave-one-out analysis was performed, where each participant was removed
147 from the SSM and reconstructed from the digitised landmarks. The average point cloud
148 was fit to the participant's landmarks using rigid-body rotation, translation, and
149 deformation along the principal components using a Limited-memory Broyden-Fletcher-
150 Goldfarb-Shanno (L-BFGS) algorithm (Liu & Nocedal 1989). The objective of the
151 optimization was to minimize the squared Euclidean distance between reconstructed and
152 target landmarks, which was performed using each set of landmarks (Fig 1). Tibia/fibula
153 geometries were also generated by isometrically scaling the average point cloud. The
154 scaling factor was the ratio of the distance between the lateral malleolus and lateral fibular
155 head markers for the average shape and target data.

156 ***Generalizability to older individuals:***

157 A dataset of bilateral lower-limb CT scans from 10 human cadavers (81.8 ± 10.7 years, 6
158 male, 4 female) was used to examine the robustness of the SSM when applied to an
159 entirely new sample. Scans were performed using a GE Revolution GSI (GE Healthcare),
160 with image acquisition settings of 120 kVp, 103 mA, in-plane resolution of 0.67 mm x
161 0.67 mm, and slice thickness of 0.625 mm. The same procedures described above were
162 used to segment and generate surface meshes of the left tibia and fibula. In one of the
163 scans, part of the left tibia/fibula was outside of the field-of-view. In this case, the right
164 tibia/fibula geometries were segmented and mirrored. Landmarks, previously defined
165 (Figure 1), were digitised on the bone surfaces. Tibia and fibula geometries were
166 reconstructed using nine and fourteen landmarks with the optimization procedure
167 described above. The average shape from the shape model was also isometrically scaled.

168 ***Musculoskeletal modelling***

169 A musculoskeletal model was implemented in MATLAB (Mathworks, Natick, MA) and

170 used to obtain moment arms of eighteen muscles attaching to the tibia and fibula
171 (Supplementary Table S3). Initial geometry and muscle parameters were obtained from
172 Arnold et al. (2010). The average shape from the SSM was rigidly aligned and scaled to
173 the generic tibia and fibula of the musculoskeletal model. The surface nodes
174 corresponding to muscle origin or insertion points were determined using a nearest
175 neighbours algorithm.

176 The musculoskeletal model was scaled using markers that were digitized on the
177 model at the lateral malleolus and head of the fibula. Reconstructed and CT-based
178 surfaces were rigidly aligned to the scaled musculoskeletal model. The musculoskeletal
179 model was then moved through a physiologic range of motion about the flexion-extension
180 axis at the knee (0° to 142° flexion) and the ankle (15° dorsiflexion to -62° plantarflexion)
181 (Soucie et al. 2011). Translations at the knee along the anterior-posterior and longitudinal
182 axes changed as a function of knee flexion; no translations were allowed at the ankle.
183 Muscle moment arms were computed using the tendon excursion method. The model was
184 positioned at each joint angle, and then perturbed by $\pm 10^\circ$. The moment arm of each
185 muscle was calculated from the change in muscle length divided by the change in joint
186 angle. Patellar ligament moment arm was calculated as the perpendicular distance from
187 the knee joint centre to the line of action of the ligament. Maximum difference in moment
188 arm compared to the model using the CT-based geometry was calculated.

189 ***Statistics:***

190 Reconstructed geometries were aligned with the participants' CT-based surface meshes
191 using a rigid iterative closest points algorithm. A nearest-neighbour algorithm was used
192 for each node to calculate RMSE and maximum distance error. Jaccard index, a measure
193 of volumetric similarity - where values range from 0 (no similarity) to 1 (identical) - was

194 also computed (Real & Vargas 1996). RMSE and maximum error were also calculated
195 for the tibia and fibula separately, and for proximal, diaphysis, and distal regions (0-20%,
196 20-80%, and 80-100% of the axial length, respectively (Edwards et al. 2013)). Statistical
197 tests were performed using SPSS (v26, IBM, NY, USA). In the leave-one-out analysis,
198 error measures for at least one of the reconstruction methods did not meet the assumption
199 of normality as defined by the Shapiro-Wilk test. Therefore, related-samples Friedman's
200 analysis of variance tests (ANOVA) were used to evaluate differences in error
201 measurements between reconstruction methods (9 landmarks, 14 landmarks, isometric
202 scaling); pairwise comparisons were used when appropriate. For the older adult dataset,
203 all error measures met the assumption of normality. In this case, repeated measures
204 ANOVAs were used to evaluate differences in error measurements between
205 reconstruction methods; again, pairwise comparisons were used when appropriate.
206 Critical values for statistical tests were adjusted for multiple comparisons using
207 Bonferroni corrections to maintain a familywise error rate of $\alpha = 0.05$.

208 **Results**

209 The first principal component in the SSM primarily captured differences in overall size
210 and explained 79.8% of the total variance in the model (Table 1). The first eight
211 components explained 96.2% of the variance (Table 1).

212 ***Sexual dimorphism:***

213 Principal component 1 discriminated between males and females ($t = 4.727$, $p < 0.001$,
214 whereby the tibia and fibula were larger in males. Principal component 1 was the only
215 mode correlated with centroid size, with $r^2 = 0.99$. Sex differences in principal
216 components 4 and 7 trended toward significance ($t = -2.231$, and -2.279 , $p = 0.031$, and
217 0.029 , respectively; Bonferroni-adjusted critical p-value = $0.05/8$ comparisons = 0.006 ;

218 Figure 2). These principal components described shape differences including larger
219 proximal epiphyseal regions, a more prominent tibial tuberosity, and more acute anterior-
220 posterior curvature in the tibia in males compared to females (Figure 2).

221 ***Reconstruction accuracy:***

222 Differences in error between reconstruction methods were observed for RMSE (χ^2
223 = 55.073, $p < 0.001$), Jaccard index ($\chi^2 = 58.098$, $p < 0.001$), and maximum error ($\chi^2 =$
224 24.927, $p < 0.001$) (Figure 3 and 4). Median (IQR) errors were smaller in SSM
225 reconstructions using nine landmarks (RMSE = 1.62 (0.35) mm, maximum error = 5.12
226 (1.63) mm) compared to isometric scaling (RMSE = 1.78 (0.62) mm, maximum error =
227 5.84 (2.62) mm, $p < 0.001$). Jaccard index was greater in SSM reconstructions from nine
228 landmarks (0.824 (0.038)) compared to isometric scaling (0.792 (0.077), $p < 0.001$). The
229 same pattern was observed between SSM reconstructions from fourteen landmarks
230 (RMSE = 1.15 (0.29) mm, maximum error = (4.82 (1.26) mm, Jaccard index = 0.833
231 (0.034)) compared to isometric scaling ($p < 0.001$). Differences between SSM
232 reconstructions using nine and fourteen landmarks were also significant, where RMSE
233 was 6.8% smaller and Jaccard index was 1.1% larger in reconstructions using fourteen
234 landmarks ($p < 0.001$). A similar pattern of results was observed when comparing errors
235 between reconstruction methods for specific regions of the tibia and fibula (see
236 Supplementary Table S1). Shape errors tended to be larger in the fibula than the tibia, and
237 in the proximal region.

238 ***Generalizability to older adults:***

239 Differences between reconstruction methods for older adults were also observed for
240 maximum error ($F = 14.047$, $p = 0.004$, $\eta^2 = 0.609$, Figure 5 and 6), and Jaccard index (F
241 = 14.379, $p = 0.004$, $\eta^2 = 0.615$). Mean (SD) maximum errors were smaller in SSM

242 reconstructions using nine landmarks (6.90 (1.00) mm) compared to isometric scaling
243 (9.21 (2.36) mm, $p = 0.005$). Jaccard index was greater in SSM reconstructions from nine
244 landmarks (0.769 (0.032)) compared to isometric scaling (0.672 (0.077), $p = 0.004$). The
245 same pattern was observed between SSM reconstructions from fourteen landmarks
246 (maximum error = 7.04 (1.03) mm, Jaccard index = 0.763 (0.037)) compared to isometric
247 scaling ($p \leq 0.005$). Regional analysis indicated that differences in maximum error were
248 driven by improvements in the proximal region of the tibia (Supplementary Table S1).
249 No differences in error measures were observed in the fibula. Pairwise comparisons
250 between SSM reconstructions and isometric scaling for RMSE for the tibia and fibula
251 combined were not significant. RMSE at the proximal and distal regions of the tibia were
252 smaller in SSM reconstructions when compared to isometric scaling ($p \leq 0.001$,
253 Supplementary Table S1). None of the error measures were different between
254 reconstructions from nine and fourteen landmarks.

255 ***Muscle moment arms***

256 In the young adult group, the reconstruction method changed the maximum difference in
257 moment arms, relative to the CT-based bones, of the semimembranosus, and the long and
258 short head of biceps femoris ($\chi^2 \geq 14.244$, $p \leq 0.001$, Supplementary Figure S1); no
259 differences in moment arms for other muscles originating from or inserting on the tibia-
260 fibular complex were observed. SSM reconstructions had smaller differences in moment
261 arms than isometric scaling for the biceps femoris long head (median (IQR): nine
262 landmarks = 2.36 (1.90) mm, fourteen landmarks = 2.45 (2.08) mm, isometric scaling =
263 3.65 (2.90) mm, $p < 0.001$) and short head (median (IQR): nine landmarks = 3.01 (2.06)
264 mm, fourteen landmarks = 2.74 (2.34) mm, isometric scaling = 3.99 (3.14) mm, $p \leq$
265 0.001). Differences for semimembranosus were smaller in reconstructions from fourteen
266 landmarks (2.61 (1.46) mm) when compared to nine landmarks (3.09 (2.24) mm) and

267 isometric scaling (3.47 (2.65) mm, $p < 0.001$). Moment arm differences in the older adults
268 were larger than for the younger adults (4.76 – 8.33 mm vs 2.36 – 3.99 mm, respectively).
269 No differences in muscle moment arms between reconstruction methods were observed
270 for the older adults.

271 **Discussion**

272 The purpose of this study was to evaluate the accuracy of tibia-fibula reconstructions from
273 anatomical bony landmarks using a SSM developed for a healthy young adult population,
274 and quantify the subsequent effects on muscle moment arms. The secondary objectives
275 were (1) to quantify sex differences in bone geometry within the young adult sample, and
276 (2) to evaluate the generalizability of the developed SSM to older adults. SSM
277 reconstructions reduced geometry errors and changed hamstring moment arms, when
278 compared to isometric scaling. On average, females had slightly narrower proximal
279 epiphyseal regions and less diaphyseal curvature. SSM reconstructions, isometric scaling,
280 and muscle moment arms in older adults were less accurate compared to the young adults.

281 Reconstruction accuracy was better in the SSM-generated models compared to
282 isometric scaling. The magnitude of the differences between SSM-generated
283 reconstructions from nine and fourteen landmarks and isometrically scaled geometries in
284 this study were somewhat small; RMSE was reduced by 0.16-0.27 mm (9-15%) and
285 maximum error was reduced by 0.72-1.02 mm (12-17%) in SSM reconstructions
286 compared to isometric scaling, depending on the number of anatomical landmarks. Nolte
287 et al. (2020) observed a larger reduction in RMSE (0.99 mm, 26%) using SSM-based
288 reconstruction with only one principal component compared to isometric scaling, and
289 even greater reductions in error were observed when more principal components were
290 used. Zhang et al (2016) observed a reduction in RMSE of 0.41 mm (11%) using SSM-

291 based reconstruction from only three bony landmarks compared to linear scaling. The low
292 reconstruction errors observed for isometric scaling in this study likely explains the
293 smaller reductions in RMSE compared to previous work. Isometric scaling was more
294 accurate in this study (RMSE = 1.78 mm) compared to Nolte et al. (2020) (RMSE = 3.87
295 mm) and Zhang et al. (2016) (RMSE = 3.63 mm). In fact, the RMSE for isometric scaling
296 in this study was also lower than SSM-based tibia-fibula reconstruction errors observed
297 by Nolte et al (2020) (2.88 mm) and Zhang et al. (2016) (3.22 mm). This could be
298 explained, in part, by the small range of young participants used to create the SSM and
299 evaluate reconstruction accuracy in this study, i.e., 18-24 years, compared to 15-92 years
300 in Zhang et al. (2016) and 23-70 years in Nolte et al. (2020) - which likely included less
301 geometric variability. The use of landmarks identified directly on the bone surface, as
302 compared to skin markers may have also contributed to more accurate results when
303 compared to isometric scaling in previous studies.

304 When the SSM based on the younger group was used to reconstruct tibia-fibula
305 geometries for the older adult group (71-98 years), errors for both isometric scaling and
306 SSM-based reconstructions were larger than errors for the young group. Isometric scaling
307 of the average young adult tibia and fibula geometries consistently underestimated cross-
308 sectional size throughout the length of the bones in older adults, which could be explained
309 by periosteal expansion (Ruff & Hayes 1988; Jee 2001). SSM reconstructions were able
310 to account for some of the variation, reducing the overestimation of cross-sectional size.
311 Although SSM-based reconstruction errors were larger in the older group than the
312 younger group, the SSM still provided 14% and 25% reductions in Jaccard index and
313 maximum error, respectively, within the older group, indicating greater robustness for
314 application to new populations when compared to isometric scaling of a generic
315 geometry.

316 Geometry errors, particularly at locations affecting joint alignment and muscle
317 attachment points, can substantially influence musculoskeletal model outcomes (Scheys
318 et al. 2008; Gerus et al. 2013; Xu et al. 2020). RMSE and maximum errors were larger in
319 the proximal epiphysis and metaphysis regions, where many muscles crossing the knee
320 insert, than in the diaphysis of the tibia and fibula (Supplementary Tables S1 and S2).
321 Moment arms of some muscles attaching in the proximal regions were different when
322 using the isometrically scaled average geometry compared to the CT-based geometry,
323 adding support to previous findings at the knee and hip (Scheys et al. 2008; Bahl et al.
324 2019). In young adults, the 9-17% reductions in geometric errors from SSM-based
325 reconstruction resulted in 25-35% reductions in maximum moment arm differences for
326 semimembranosus and biceps femoris long and short heads. Previous work has
327 demonstrated substantial sensitivity of muscle forces and joint contact forces to geometry
328 (image-based vs. generic models) and perturbations of muscle insertion points and
329 moment arms on the order of ± 1 cm (Carbone et al. 2012; Gerus et al. 2013; Xu et al.
330 2020). The absolute changes in muscle point and maximum moment arm differences
331 between SSM and isometric scaling methods in this study were an order of magnitude
332 smaller (≤ 1.3 mm). These differences may not translate to significant changes in muscle
333 forces or joint contact forces, but this must be confirmed in future work. In the older
334 adults, moment arm and muscle origin/insertion point differences relative to the CT-based
335 model were larger: up to 8 mm and 22 mm, respectively (Supplementary Tables S3 and
336 S4). However, moment arm differences were not changed between reconstruction
337 methods. Although SSM-reconstruction improved geometric accuracy, it was not better
338 than isometric scaling of a generic model for musculoskeletal modelling application in an
339 outside population. A SSM including older adults in the training set would provide better
340 results.

341 In addition to age, sex is a factor known to influence bone geometry. In this study,
342 the scores for three principal components differentiated between sexes. While not
343 statistically significant, likely due to the extremely conservative Bonferroni adjustment
344 for eight comparisons, trends were observed in principal components 4 and 7. Shape
345 differences were subtle, as these principal components accounted for very small
346 percentages (3.15% and 1.19%) of variance in the SSM and there was overlap in the
347 principal component scores (Figure 2). These results are consistent with the observations
348 of Brzobohatá et al. (2016).

349 A limitation of this study is that landmarks were identified directly on the bone
350 surface. In the young adult group, using only the ‘palpable’ landmarks slightly reduced
351 accuracy when compared to reconstructions from all 14 landmarks, but this was still 4-
352 12% better than isometric scaling. This illustrates the potential for a subset of landmarks
353 that might be used to predict tibia-fibula geometry without the use medical imaging,
354 perhaps using skin-mounted markers collected during a static motion capture trial. Of
355 course, estimating the soft-tissue offset between skin mounted markers and bony
356 landmarks and landmark placement errors may introduce additional uncertainty. Mean
357 soft tissue offsets of 4.8-7.7 mm and skin marker placement inter-examiner precision of
358 11-20 mm have been reported for anatomical landmarks on the shank (Della Croce et al.
359 1999; Nolte et al. 2020). Methods have been proposed to reduce errors and improve
360 reliability for skin marker placement (Osis et al. 2016; Hutchinson et al. 2018). Larger
361 errors may be observed for markers on the tibia shaft, which would be placed using a
362 measuring tape to identify 25, 50, and 75% positions along the tibial crest between the
363 lateral malleolus and fibular head markers. An approach allowing axial movement of the
364 tibial crest markers (Nolte et al. 2020) may reduce the effects of this source of error.
365 Encouragingly, Nolte et al. (2020) observed small standard deviations (0.90-2.99 mm) in

366 soft-tissue offsets for seven markers on the shank, six of which were the same or similar
367 to landmarks used in this study. The authors reported that no differences in RMSE were
368 observed between reconstructions from bone landmarks and skin markers digitised using
369 an optical motion capture system, with or without soft-tissue offset corrections, when one
370 or two principal components were used. This provides some confidence that the SSM
371 developed in this study could be used to reconstruct tibia-fibula geometries using skin-
372 mounted markers, although additional work is needed to determine the number of
373 principal components that could be used and to quantify the model-specific reconstruction
374 accuracy.

375 The training set used in this study to create the SSM, which was composed of
376 young active adults with no musculoskeletal abnormalities, may limit the applicability of
377 the model to clinical or paediatric populations. Ethnicity is also a factor influencing bone
378 geometry (Mahfouz et al. 2012). Unfortunately, ethnicity information was not collected,
379 although most participants appeared to be of Caucasian descent.

380 In conclusion, within a young physically active population, and using an average
381 model specific to that population, isometric scaling provided predictions of tibia and
382 fibula bone geometry with low error. The developed SSM produced estimated tibia and
383 fibula geometries from bony landmarks with even greater accuracy. However, this only
384 affected the moment arms of three muscles. Geometry errors were larger in the older adult
385 group. Although SSM-based reconstruction using a model trained on young adults was
386 able to account for some geometric variation in an outside population, it was not
387 sufficiently robust to alter musculoskeletal model parameters compared to a scaled
388 generic model.

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393 on the older adults.

394 **Declaration of Interest**

395 The authors have no potential conflicts of interest to report.

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506 Table 1. Percent of total variance explained by principal components 1-8.

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Principal component	1	2	3	4	5	6	7	8
Variance explained (% of total)	79.8	4.7	3.6	3.1	1.7	1.4	1.2	0.7
Cumulative variance explained (% of total)	79.8	84.5	88.1	91.2	92.9	94.3	95.5	96.2

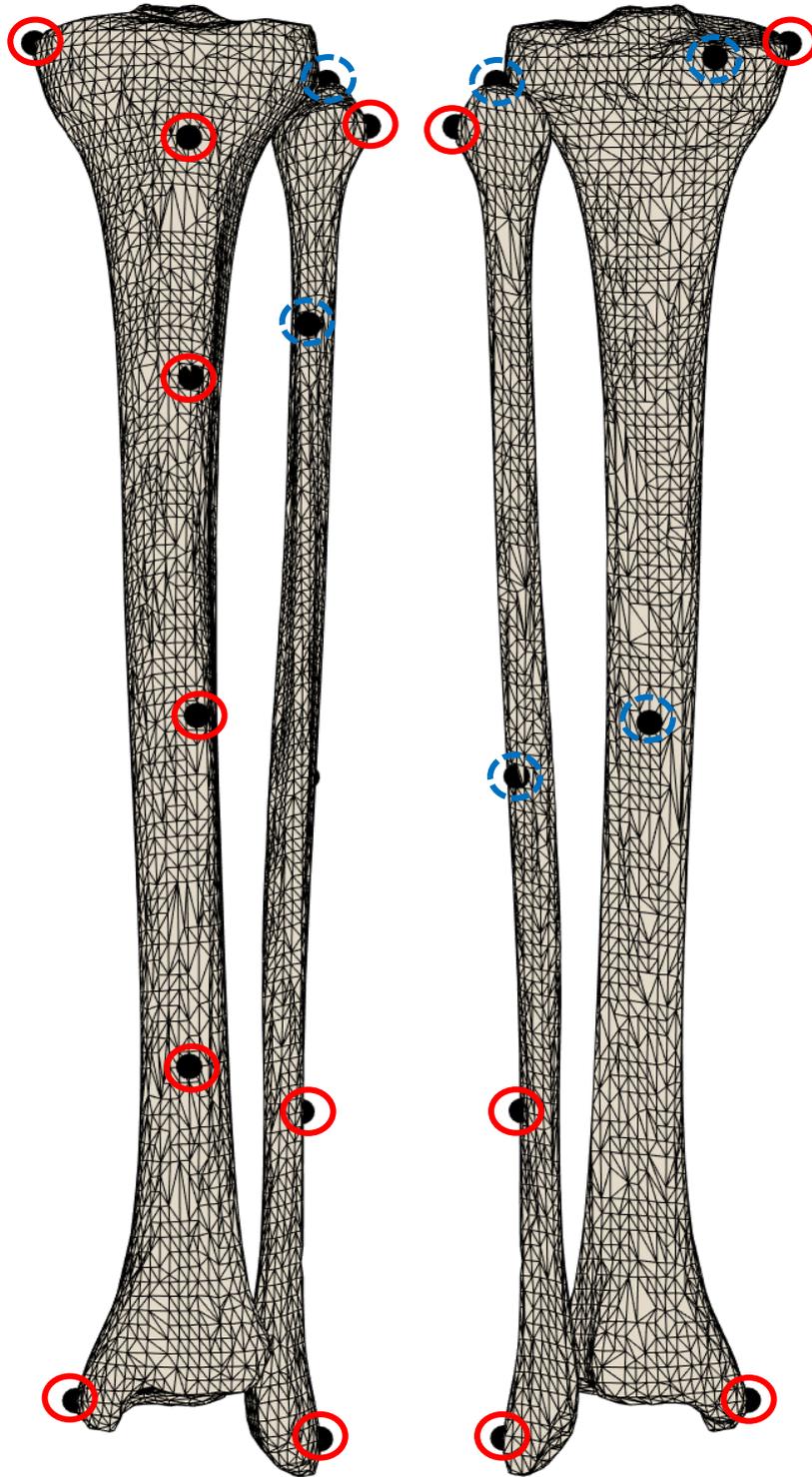
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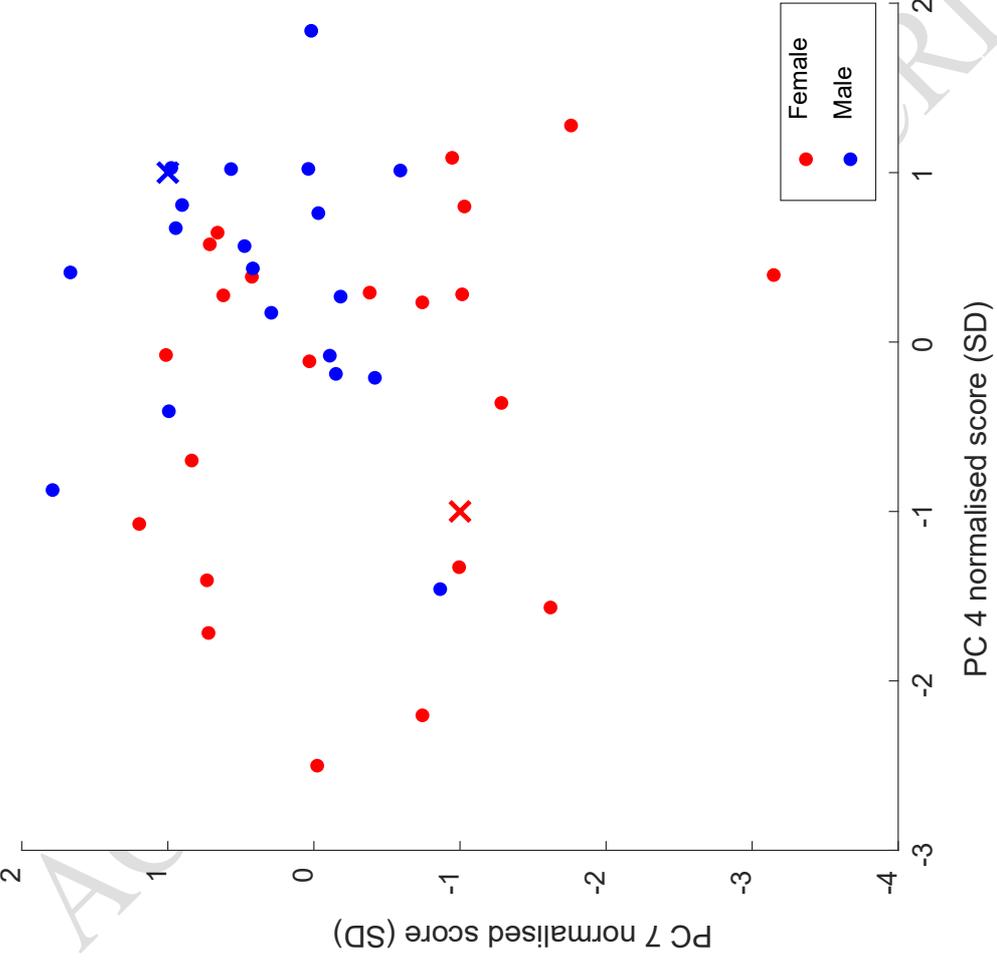


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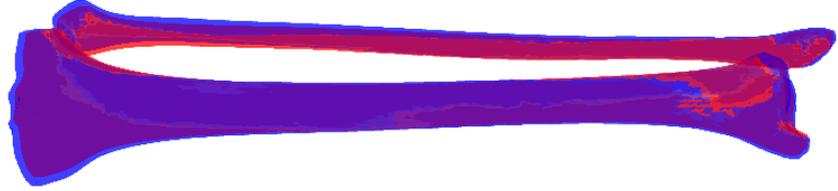
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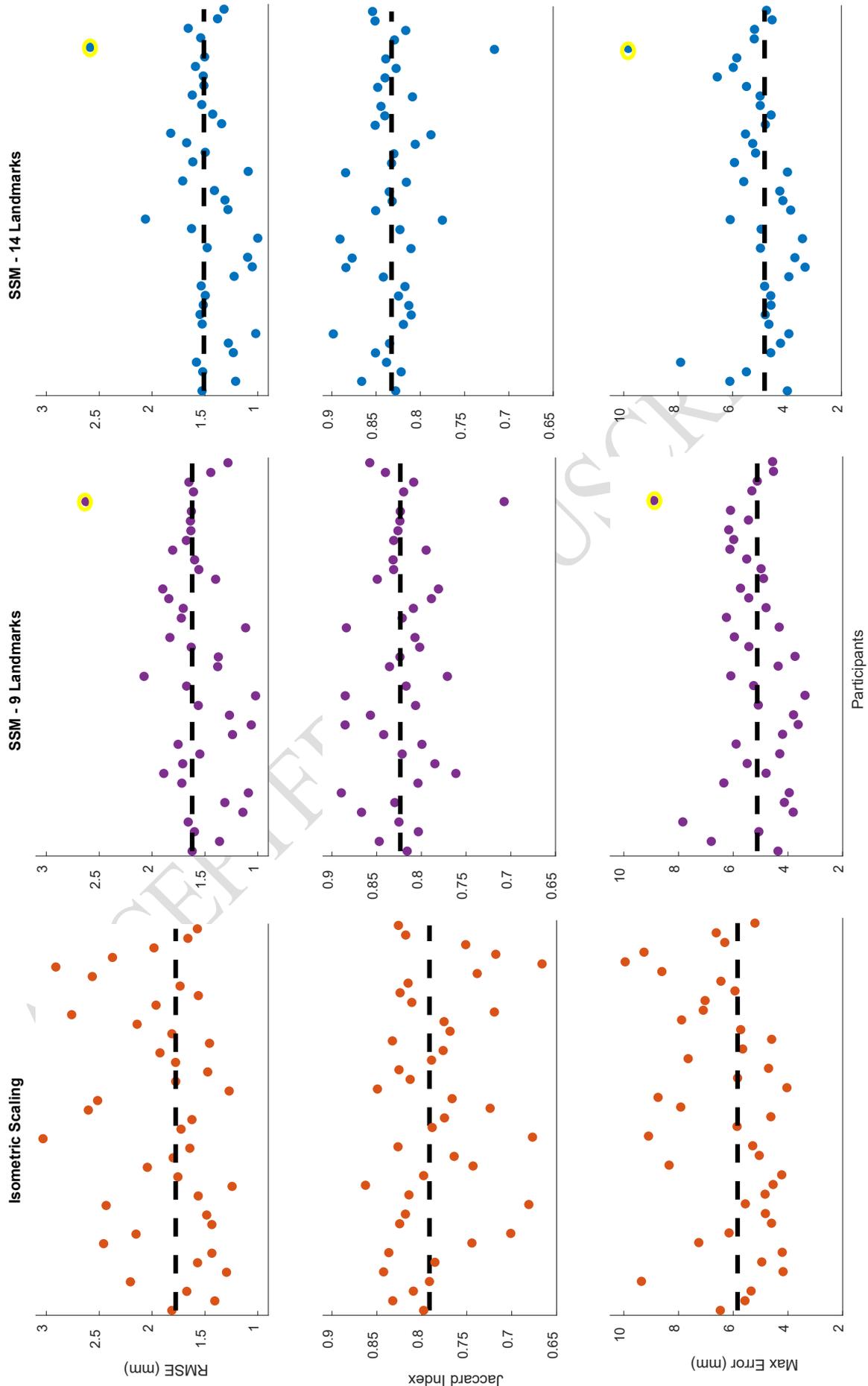


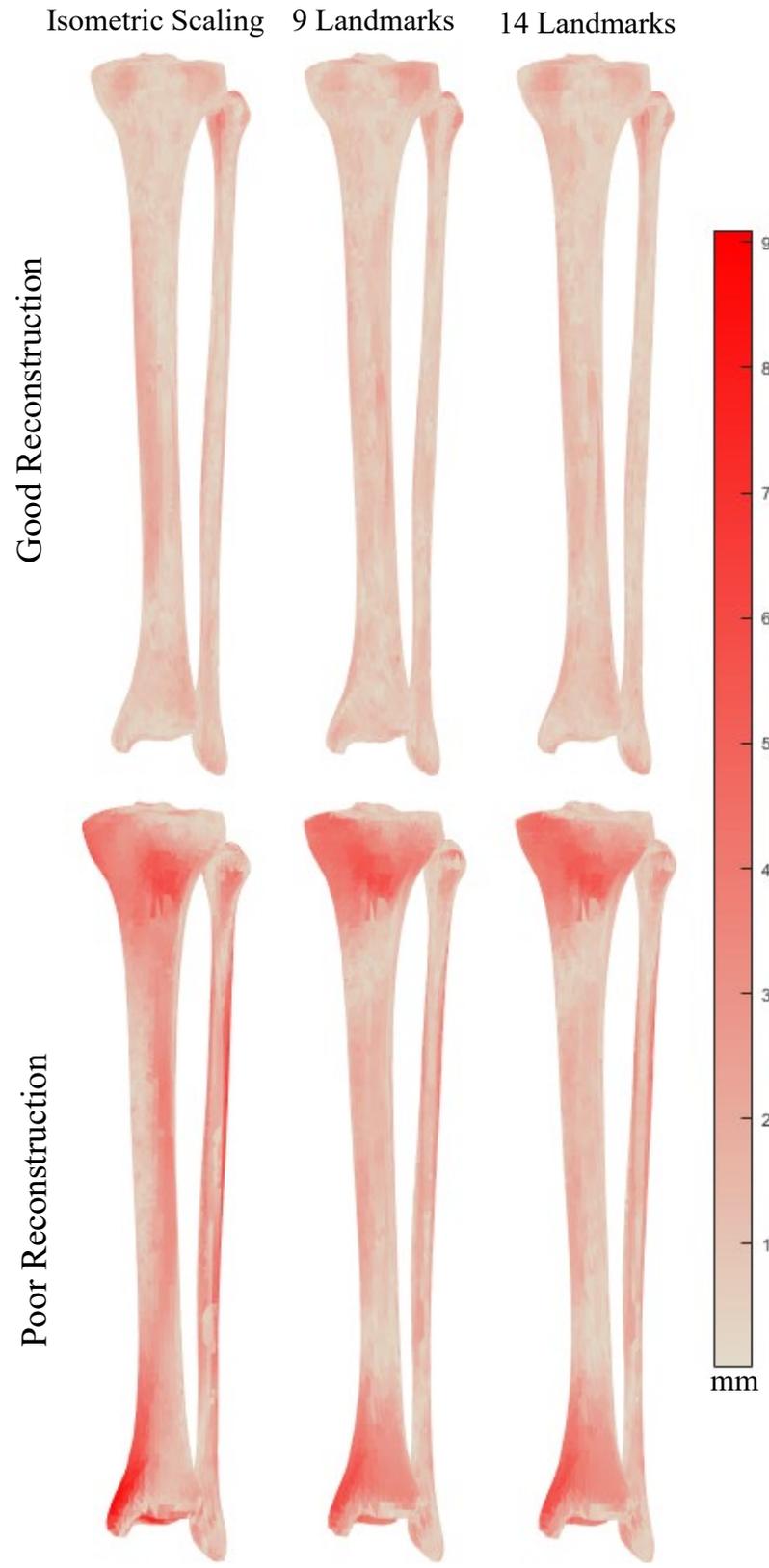
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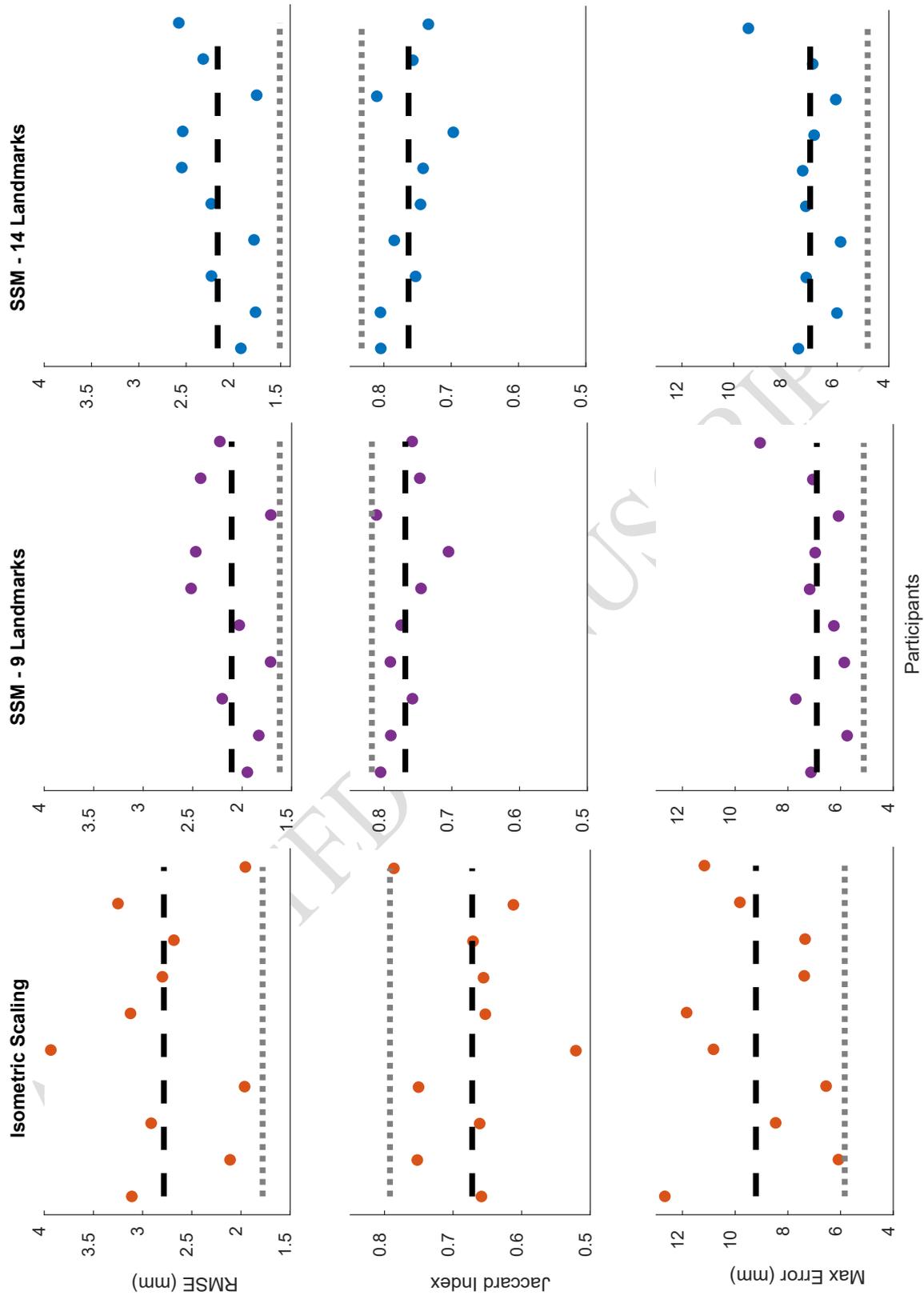
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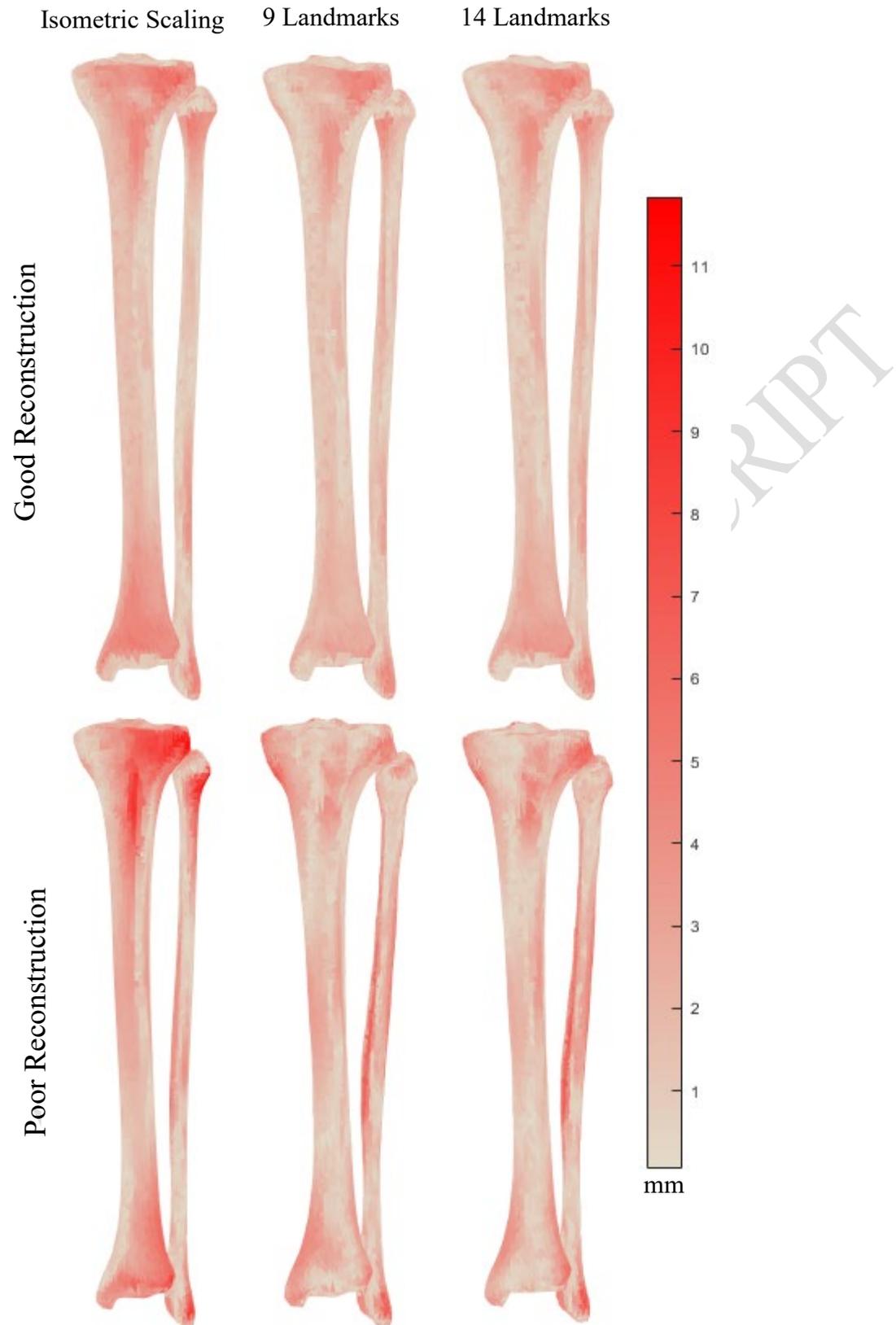
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523 Figure 1. Landmarks used for reconstructions. The subset of nine palpable landmarks
524 are circled in red. The five non-palpable landmarks are circled in blue (dashed line).

525 Figure 2. (Left) Scatterplot of principal components 4 and 7 normalised scores. Red
526 circles (female) and blue squares (male) represent individual participants. The x's
527 represent the average shape + (blue) or - (red) 1 standard deviation (SD) for both
528 principal components (PC) 4 and 7. (Left) Representations of the tibia-fibula complex
529 geometry of the blue and red x's. Sex differences in shape were very subtle. ± 1 SD was
530 larger than mean normalised scores for females (PC4 = -0.31, PC7 = -0.31) and males
531 (PC4 = 0.36, PC7 = 0.35) and was used to more easily visualise differences.

532 Figure 3. Errors and volume similarity of tibia and fibula geometries predicted using
533 isometric scaling or SSM-landmark reconstruction methods compared to CT data. Dots
534 represent individual participants. The highlighted dots are an outlier. The dashed line
535 represents the median. Differences between SSM-landmark methods and isometric
536 scaling were significant for all three measures. Differences between 9 and 14 landmark
537 reconstructions were significant for RMSE and Jaccard index.

538 Figure 4. Good (top, participant 14) and poor (bottom, participant 19) reconstructions
539 for isometric scaling and SSM-landmark methods.

540 Figure 5. Errors and volume similarity of tibia and fibula geometries for older
541 individuals predicted using isometric scaling or SSM-landmark reconstruction methods
542 compared to CT data. Dots represent individual participants. The black dashed line
543 represents the mean. Differences between SSM-landmark methods and isometric
544 scaling were significant for Jaccard index and maximum error. Errors were not different
545 between 9 and 14 landmark reconstructions. The dotted grey line represents the median
546 of the young adult group.

547 Figure 6. Good (top, participant 4) and poor (bottom, participant 6) reconstructions of
548 older participants for isometric scaling and SSM-landmark methods.